University of Waterloo, Department of Statistics and Actuarial Science

Joint Rutgers-CMU-Waterloo PhD Topic Course

STAT946/ACTSC991 Winter 2021
Game-theoretic statistical inference: betting, e-values and martingales

Time
Jan 22 – Apr 30 (Optional after Apr 9 for Waterloo students)
Fridays, 10am - 1pm EST (with short break 11:45-12:00)

Instructor
Ruodu Wang (http://sas.uwaterloo.ca/~wang/) Email: wang@uwaterloo.ca

Description
This course is a joint Rutgers-CMU-Waterloo PhD topic course which will be taught online (via Zoom) by Ruodu Wang (University of Waterloo), Glenn Shafer (Rutgers University) and Aaditya Ramdas (Carnegie Mellon University). We will study the game-theoretic foundation for statistics and its applications to prediction, testing and estimation. It will distinctively employ modern concepts around betting, e-values, and martingales, effectively bridging Bayesian, frequentist and model-free or adversarial perspectives on these topics. The course is based on very recent research results in a rapidly developing field.

Course website
https://www.stat.cmu.edu/~aramdas/betting/b21.html
The course website contains the course schedule and download links of all reading materials.

Prerequisites
Basic graduate level (or advanced undergraduate) training in statistics or probability.

Office hours
Remotely by appointment

Additional information
- Glenn Shafer (http://www.glennshafer.com/), University Professor, Rutgers Business School, Rutgers University
- Aaditya Ramdas (http://stat.cmu.edu/~aramdas/), Assistant Professor, Department of Statistics and Data Science, Machine Learning Department, Carnegie Mellon University
- Ruodu Wang (http://sas.uwaterloo.ca/~wang/), University Research Chair and Associate Professor, Department of Statistics and Actuarial Science, University of Waterloo
Zoom link
The zoom link will be available later.

Office hours (Waterloo students only)
Every Wednesday 10am to 11am (EST) I will host office hours on WebEx (the weeks of Jan 25 – April 5). The information can be found on Learn.

Basis of grading
- Homework 20%
- Class participation 30% (evaluated via questions from pre-class reading)
- Research project and oral presentation 50%

Detailed schedule

   Testing by betting. RSS paper [S1] with discussion and response

   Classical statistics with betting protocols. [SV Chapter 10, S2]

   E-values vs p-values: calibration, combination, and closed testing [VW1]

   Martingales, likelihood ratios, e-values and betting scores [RRLK, WRB]

   Composite, nonparametric null testing using nonnegative supermartingales [HRMS1]
   (Reading Week in Waterloo. Waterloo students can watch the video later if they choose not to attend the lecture this week.)

   False discovery rate control with e-values [WR1]

Week 7. March 5. Glenn Shafer.
   Upper and lower expectations. Chapter 6, Shafer and Vovk [SV]

   Abstract theory of testing. Chapters 7 and 8, Shafer and Vovk [SV]

   Spring Break in the US. RW hosts presentations for Waterloo students in this week.

Discovery matrices with e-values [VW2, VW3]

Nonparametric estimation via confidence sequences [HRMS2, WR2, WR3]

Universality of martingales in "safe, anytime-valid testing/estimation" [RRLK, WRB]

(The following weeks will be optional for Waterloo students; they are encouraged to attend these lectures, although their grades do not depend on lectures after April 9.)

P*-values and randomized tests: A bridge between p-values and e-values [W]

Week 14. April 23. To be decided (possibly a guest lecturer)

Week 15. April 30. Student presentations and high-level discussion of the course

Reading materials (see the course website for updates and links)

[HRMS1] Time-uniform Chernoff bounds via nonnegative supermartingales.


[S1] Testing by betting: A strategy for statistical and scientific communication, with discussion and response.

[S2] How the game-theoretic foundation for probability resolves the Bayesian vs. frequentist standoff. G. Shafer. preprint, 2020  preprint

G. Shafer and V. Vovk, Wiley 2019

[VW1] E-values: Calibration, combination, and applications.

[VW2] True and false discoveries with e-values.
V. Vovk, R. Wang. ArXiv, 2020, [arxiv]

[VW3] True and false discoveries with independent e-values.
V. Vovk, R. Wang. ArXiv, 2020, [arxiv]

R. Wang. ArXiv, 2020, [arxiv]

[WR1] False discovery rate control with e-values.
R. Wang, A. Ramdas. ArXiv, 2020, [arxiv]

[WR2] Confidence sequences for sampling without replacement.

I. Waudby-Smith, A. Ramdas. ArXiv, 2020, [arxiv]

[WRS] Universal inference.
L. Wasserman, A. Ramdas, S. Balakrishnan. PNAS, 2020, [arxiv proc]